



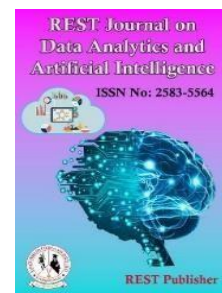
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Assessing Statistical Models for Predictive Accuracy of PM_{2.5} Pollution in Delhi, India

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Abstract: Particulate matter is a significant atmospheric pollutant that poses substantial health risks. Reliable and precise air quality forecasts are essential for the timely implementation of preventive measures to minimize these health risks. This study examines the effectiveness of various statistical methods in forecasting long-term trends of particulate matter (PM_{2.5}) pollution. Using historical data from government-operated monitoring stations in Delhi, the research applies a range of time-series analysis techniques to identify patterns and predict future pollution levels. The analysis reveals that the Seasonal Autoregressive Integrated Moving Average model with exogenous variables (SARIMAX) significantly outperforms other models, such as ARIMA, SARIMA, and ARIMA with exogenous variables (ARIMAX). The exceptional performance of SARIMAX demonstrates its potential as a robust early warning system, which can facilitate the implementation of preventive measures to mitigate the impact of pollution on public health. This emphasizes the model's significance in supporting proactive environmental and health policy strategies.

Keywords: Particulate matter; PM_{2.5}; Forecasting; SARIMA; ARIMA; SARIMAX; ARIMAX

1. INTRODUCTION

The rapid urbanization and development of cities pose significant challenges, leading to population surges and inadequate public services. This uncontrolled urban expansion in developing countries pressures natural resources, resulting in environmental degradation at multiple levels [1]. Among global environmental concerns, ambient (outdoor) air pollution is notably exacerbated by these unsustainable practices. Poor ambient air quality, due to increased levels of pollutants, is primarily attributed to anthropogenic emissions from vehicles, industry, construction, and domestic burning, though natural emissions also contribute [2], [3]. These sources release particulate matter (PM₁₀, PM_{2.5}) and gaseous pollutants like nitrogen and sulfur oxides, carbon monoxide, and ozone [4]. The concentrations of these pollutants are influenced by synoptic patterns and meteorological parameters [5].

Concerns about poor air quality in India have surged recently due to its adverse effects on human health, agricultural productivity, and the economy [6], [7]. India's rapid urban and industrial development has led to some of the world's most polluted air. With 34% of its 1.3 billion population living in urban areas, air quality is deteriorating rapidly [8], [9]. A study by [10] highlighted that over 70% of India's population is exposed to particulate concentrations exceeding National Ambient Air Quality Standards (NAAQS), contributing to increased mortality and morbidity, with approximately 0.7 million deaths annually linked to ambient air pollution. The economic impact of poor air quality accounts for about 1.4% of the GDP, including expenditures on health issues related to pollution [11].

Many metropolitan and Tier-I cities in India, such as Delhi, Kolkata, and Mumbai, are experiencing worsening air quality [12]. This deterioration is due to various factors, including vehicle exhaust emissions (VEEs), resuspended dust, biomass burning, and industrial pollution [13], [14]. Consequently, these cities are struggling to meet health-based air quality standards. Regularly examining changes in air pollutant concentrations is essential to develop reliable solutions to mitigate and assess the health and environmental risks associated with poor air quality in urban areas [15]. Predicting and forecasting air pollution is crucial not only for enabling residents to

plan their daily activities and avoid high-pollution areas but also for supporting urban planning and public health strategies [16]. Time series modeling is pivotal in this process, offering benefits such as data cleaning, understanding, and forecasting. As a vital quantitative technique, time series forecasting involves collecting and analyzing historical data to develop models that predict future scenarios [17]. Given its significance, research on pollution forecasting has become a critical area in environmental protection, aiming to evaluate and implement necessary measures to mitigate the long-term effects of pollution [18].

This research addresses significant gaps in predicting and forecasting PM_{2.5} levels in Delhi by conducting a comparative analysis of traditional (ARIMA & SARIMA) and advanced (ARIMAX & SARIMAX) time series models. The study explores spatio-temporal trends in PM_{2.5} data from 39 monitoring stations (2019-2023). It evaluates model accuracy with metrics like RMSE and R-squared, integrating a broad range of exogenous variables such as temperature, wind speed, rainfall, solar radiation, barometric pressure, and humidity. This comprehensive approach aims to improve predictive accuracy and provide actionable insights for policymakers and urban planners, enhancing air quality forecasting in megacities prone to pollution.

2. METHODS

A. Location Description: Delhi, situated at 28°34'N and 77°12'E, is India's capital city. As of the 2011 census, it had a population of 16.8 million and a growth rate of 1.92%, making it India's second-largest city by population. The city's climate is semi-arid and subtropical, with prevailing wind patterns mainly from the west and northwest. The average wind speed annually is between 0.9 to 2 m/s, according to [19]. Temperature-wise, Delhi has an average yearly temperature of 31.5°C. During the hot months from March to June, temperatures can soar up to 45°C. In contrast, temperatures significantly drop during the winter months of December and January, which helps in trapping emissions and raising pollution levels [20]. The monsoon season, typically from July to September, brings most of Delhi's rainfall, significantly influencing the city's annual weather patterns.

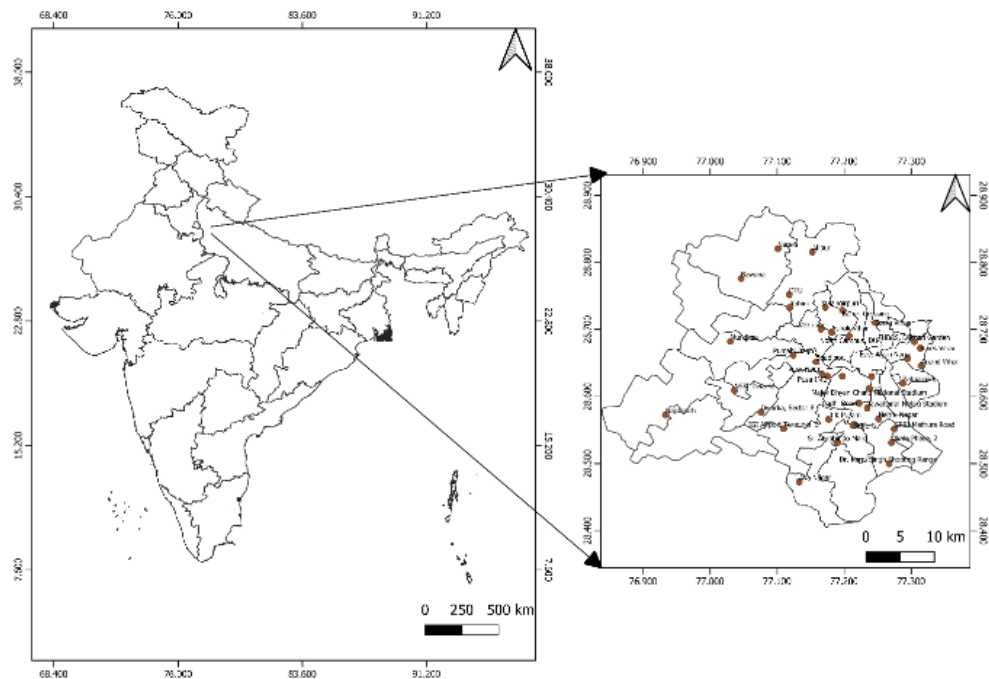


FIGURE 1. The location of Delhi city

B. Data Collection and Pre-Processing: Daily PM_{2.5} concentration data were collected from the Central Pollution Control Board's digital repository (<http://app.cpcbcr.com/ccr/#/login>) for 39 monitoring stations across Delhi. This dataset covers five years, starting January 1, 2019, and ending December 31, 2023. PM_{2.5} levels are measured using gravimetric, TEOM, or beta attenuation methods at stations managed by the CPCB, IMD, and DPCC. These measurements adhere to the [21] for ambient air pollutant measurement. Regular calibration of the monitors by the managing authorities ensures data reliability [3], [22].

Meteorological data, including daily measurements of temperature, humidity, wind speed, rainfall, solar radiation, and barometric pressure, were also sourced from the same CPCB repository for the same stations. These instruments are regularly calibrated according to guidelines to ensure data accuracy. Data pre-processing has been conducted to improve the quality and usability of this information.

To ensure robust analysis, we pre-processed air quality and meteorological data from 39 Delhi stations, spanning 2019 to 2023. We eliminated stations with less than 75% data completeness, interpolated isolated missing values, and applied mean imputation for continuous gaps using historical seasonal patterns. Meteorological data from nearby stations filled gaps, and monthly data aggregation allowed for effective trend analysis and model development

C. Data Analysis: We analysed PM_{2.5} concentrations at various Delhi stations from 2019 to 2023 using both traditional and advanced time series models to adapt to the dynamic air quality data. Traditional models like ARIMA and SARIMA were used to identify data patterns, while ARIMAX and SARIMAX incorporated meteorological variables like temperature, wind speed, and humidity to assess external effects on PM_{2.5} levels [23], [24].

Before model application, we confirmed data stationarity using the Augmented Dickey-Fuller (ADF) test, as recommended by [25]. This step ensured the data's mean, variance, and covariance were constant over time, a crucial factor since non-stationary data can lead to inaccurate time series analysis results.

Our study employed ARIMA and SARIMA models to predict PM_{2.5} levels, adapting them to capture both the typical and seasonal variations in air quality data. These models were fine-tuned using the `auto_arma` function from the `pmdarima` library, optimizing parameter selection based on the Akaike Information Criterion (AIC) to ensure the best model fit [26].

ARIMA, widely used for forecasting stationary time series, combines three elements: autoregressive (AR), differencing (I), and moving average (MA). The AR component uses previous values to predict future ones with p as the number of lags. Differencing, denoted by d , stabilizes the series, while MA, represented by q , models the error using past forecast errors.

$$\left(1 - \sum_{i=1}^p \phi_i L^i\right) (1 - L)^d Y_t = \left(1 + \sum_{j=1}^q \theta_j L^j\right) \varepsilon_t$$

where ϕ_i and θ_j are the coefficients for the AR and MA parts, L is the lag operator, Y_t is time series data at time t , and ε_t is the noise [27]. Other models incorporated in the study are extension of the ARIMA model which induces seasonality (SARIMA) as well as exogenous features (ARIMAX and SARIMAX)

To broaden our analysis, we integrated ARIMAX and SARIMAX models, which included meteorological factors as exogenous variables, enhancing the predictive accuracy by accounting for external environmental impacts. Parameter optimization was achieved using the `auto_arma` function, with additional tests on variable combinations to pinpoint those most impactful on model performance. Our comprehensive and methodical approach in fine-tuning the models allowed us to leverage time series analysis effectively, providing reliable forecasts of PM_{2.5} concentrations. This helped us not only understand but also predict air quality trends, supporting urban air quality management strategies.

In the final analysis phase, we assessed the models' performance using R-squared and Root Mean Square Error (RMSE) across each station to identify the most accurate models. The best models were then applied to test datasets to validate their effectiveness in real-world scenarios, proving essential for enhancing air quality management [28], [29]

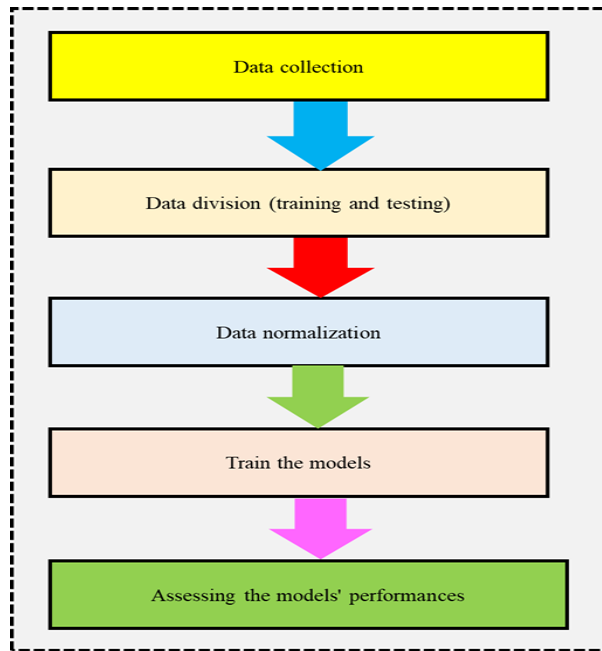


FIGURE 2. Model development steps.

3. RESULT AND DISCUSSION

We conducted an extensive comparative study of four time series models—ARIMA, ARIMAX, SARIMA, and SARIMAX—to predict $PM_{2.5}$ levels at the air quality monitoring network in Delhi from 2019 to 2023. Utilizing detailed datasets, we evaluate each model's effectiveness using the Root Mean Square Error (RMSE) and R-squared (R^2) metrics, which measure the accuracy of the predictions and the variance explained by the models, respectively.

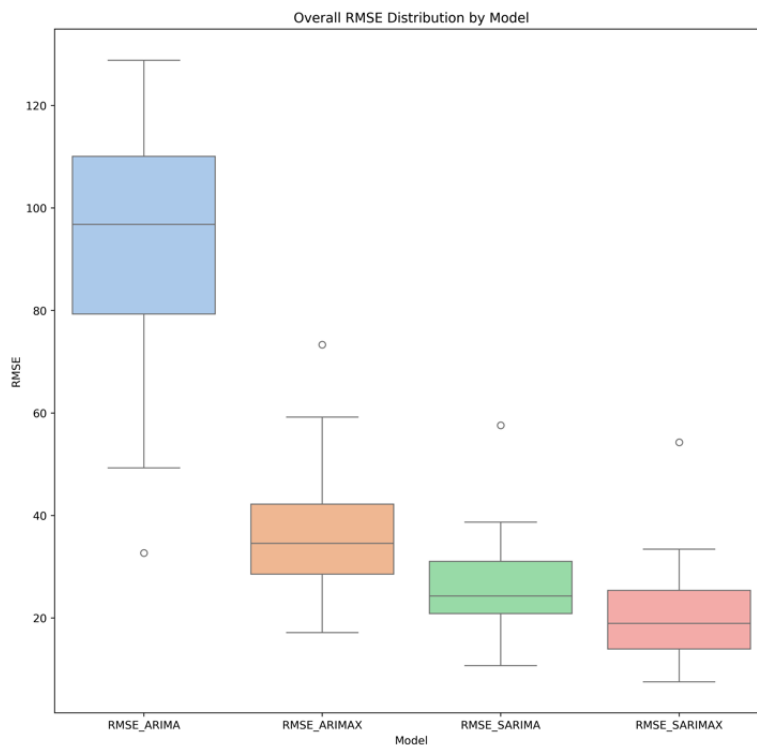


FIGURE 3. Overall RMSE of Time Series Models for $PM_{2.5}$ at Delhi Monitoring Stations.

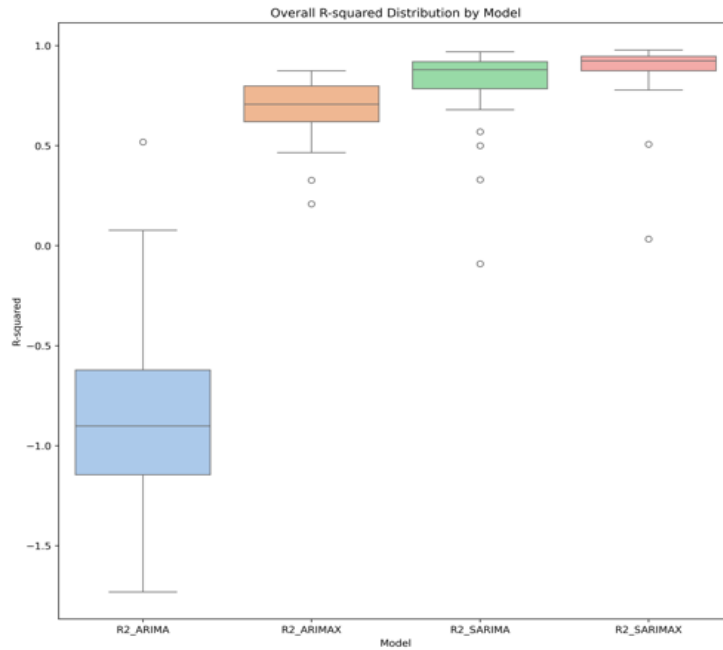


FIGURE 4. Overall R2_Score of Time Series Models for PM2.5 at Delhi Monitoring Stations

The distribution of RMSE and R² values for each model type, as visualized in the box plots (Figure 3 & 4), reveals significant insights into their predictive capabilities. The SARIMAX model generally exhibited the most favorable performance, achieving the lowest RMSE values across most stations, suggesting a robust fit to the data. Conversely, the ARIMA model frequently showed higher RMSE values, indicating a less accurate fit. This pattern was consistent with the R-squared values, where SARIMAX models also tended to explain a higher variance, demonstrating superior predictive power compared to the ARIMA models.

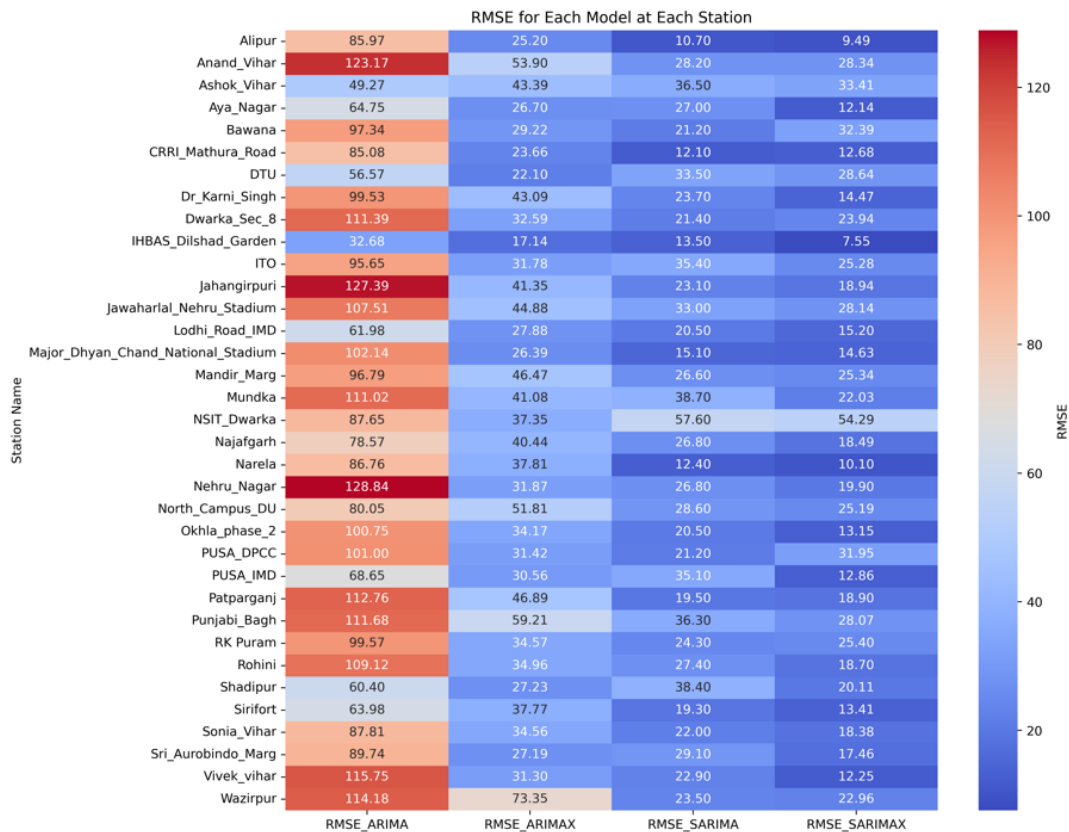


FIGURE 5. RMSE Scores for Time Series Models at Each Station

Detailed examination of model performance at each station further highlighted the consistency of SARIMAX models in achieving lower RMSE and higher R² values. For instance, at the Alipur station, the SARIMAX model produced an RMSE of 9.49 and an R² of 0.98, markedly outperforming other models. Similarly, at the Vivek Vihar, which is critical given its traffic density, the SARIMAX model not only achieved the RMSE of 12.25 but also managed an R² of 0.97, underscoring its effectiveness in high pollution areas.

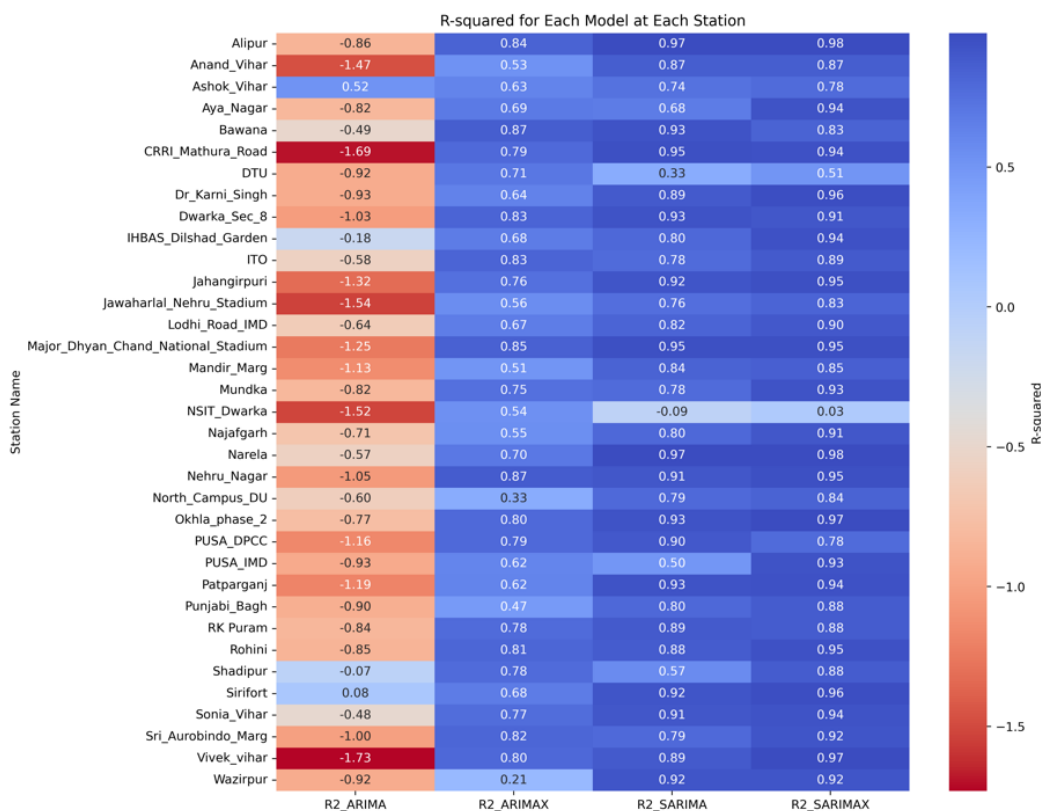


FIGURE 6. R2 Scores for Time Series Models at Each Station

The integration of exogenous variables in the ARIMAX and SARIMAX models significantly impacted their performance. Variables such as ambient temperature ('amb_temp'), wind speed ('wind_spd'), and rainfall were frequently used across stations, enhancing model predictions. The station-specific results illustrate that the inclusion of variables like solar radiation ('sol_rad') and barometric pressure ('bar_press') in the SARIMAX model notably improved its predictive accuracy at stations like Jawaharlal Nehru Stadium and Wazirpur, respectively.

Our evaluation revealed clear differences in performance among traditional (ARIMA and SARIMA) versus advanced (ARIMAX and SARIMAX) time series models for predicting PM_{2.5} levels. Traditional models effectively identified seasonal trends but fell short in accounting for external factors that critically affect pollution levels. This was evident from their generally higher RMSE and lower R² values. On the other hand, ARIMAX and SARIMAX models incorporated crucial meteorological data as exogenous variables, markedly improving their predictive capabilities. The SARIMAX model, in particular, displayed enhanced accuracy, proving highly effective in managing complex urban air quality scenarios and deepening our comprehension of air pollution dynamics in large cities like Delhi.

This study not only addresses a significant gap in environmental modeling but also lays a methodological foundation for future research, aiming to enhance the predictive accuracy and real-world utility of air quality forecasts in urban areas. It recommends expanding the integration of broader datasets, including real-time traffic, biomass burning, construction activities, and industrial outputs, to refine predictions. Additionally, it suggests enhancing collaborations with local communities and stakeholders, aligning scientific efforts with urban governance to create more sustainable, health-conscious urban environments.

TABLE 1. Station Specific Optimal Time Series Model

| Station Name | Best Model | Model Paramete | Exogenous Features |
|------------------------------------|------------|---------------------------|--|
| Alipur | SARIMAX | ((0, 1, 1), | ('wind_spd', 'rainfall') |
| Anand_Vihar | SARIMA | (0, 1, 0)x(1, 0, 1, | None |
| Ashok_Vihar | SARIMAX | ((0, 1, 0), (1, 0, 0), | ('amb_temp', 'rainfall') |
| Aya_Nagar | SARIMAX | ((1, 1, 2), (1, 0, 2), | ('amb_temp', 'wind_spd', 'sol_rad') |
| Bawana | SARIMA | (0, 1, 0)x(2, 0, 0, | None |
| CRRM_Mathura_Road | SARIMA | (0, 1, 0)x(2, 0, 0, | None |
| DTU | ARIMAX | (0, 1, 1), ((2, 1, 2), | ('amb_temp', 'rel_hum', 'wind_spd') |
| Dr_Karni_Singh | SARIMAX | (1, 0, 1), (1, 1, | None |
| Dwarka_Sec_8 | SARIMA | 0)x(2, 0, 1), ((1, 0, 0), | None |
| IHBAS_Dilshad_Garden | SARIMAX | (2, 0, 0, 12)) | ('amb_temp', 'rainfall', 'bar_press') |
| ITO | SARIMAX | ((0, 1, 1), (1, 0, 1, | ('amb_temp', 'wind_spd', 'rainfall', 'sol_rad') |
| Jahangirpuri | SARIMAX | ((3, 1, 0), (2, 1, 1, | ('wind_spd', 'rainfall') |
| Jawaharlal_Nehru_Stadium | SARIMAX | ((0, 1, 0), (1, 0, 2, | None |
| Lodhi_Road_IMD | SARIMAX | 12)) | ('rel_hum', 'sol_rad') |
| Major_Dhyan_Chand_National_Stadium | SARIMAX | ((0, 1, 0), (2, 1, 0, | ('rainfall', 'sol_rad', 'bar_press') |
| Mandir_Marg | SARIMAX | 12)) | ('amb_temp', 'rel_hum', 'wind_spd', 'rainfall', 'sol_rad') |
| Mundka | SARIMAX | ((0, 1, 0), (2, 0, 0, | ('rel_hum', 'sol_rad') |
| NSIT_Dwarka | ARIMAX | ((2, 1, 2), (0, 1, 1, | ('amb_temp', 'rel_hum', 'wind_spd', 'rainfall', 'sol_rad') |
| Najafgarh | SARIMAX | (0, 1, 1), ((3, 1, 1), | None |
| Narela | SARIMAX | (1, 0, 1), ((0, 1, 2), | ('sol_rad',) |
| Nehru_Nagar | SARIMAX | (0, 1, 1), ((2, 1, 2), | ('amb_temp', 'wind_spd', 'rainfall') |
| North_Campus_DU | SARIMAX | (2, 0, 0), ((2, 1, 0), | ('rainfall', 'sol_rad') |
| Okhla_phase_2 | SARIMAX | (2, 1, 0), (2, 1, 0, | ('rel_hum', 'rainfall') |
| PUSA_DPCC | SARIMA | ((0, 1, 1), (2, 0, 1, | ('amb_temp', 'sol_rad', 'bar_press') |
| PUSA_IMD | SARIMAX | (0, 1, 0)x(1, 0, 2, | None |
| Patparganj | SARIMAX | ((0, 1, 0), (1, 0, 2, | ('amb_temp', 'rainfall') |
| Punjabi_Bagh | SARIMAX | ((2, 1, 0), (2, 1, 0), | None |
| RK_Puram | SARIMA | (2, 1, 1), ((0, 1, 0), | ('bar_press',) |
| Rohini | SARIMAX | (1, 0, 1), ((1, 0, 1), | ('amb_temp', 'rel_hum', 'rainfall', 'bar_press') |
| Shadipur | SARIMAX | (0, 1, 1), ((1, 0, 1), | None |
| Sirifort | SARIMAX | ((0, 1, 1), (1, 0, 1, | ('rainfall',) |
| Sonia_Vihar | SARIMAX | ((0, 1, 1), (1, 0, 1, | ('wind_spd', 'rainfall', 'sol_rad', 'bar_press') |
| Sri_Aurobindo_Marg | SARIMAX | ((0, 0, 2), ((0, 1, 0), | ('wind_spd',) |
| Vivek_vihar | SARIMAX | (2, 1, 0), ((0, 1, 0), | ('wind_spd', 'rainfall', 'sol_rad') |
| Wazirpur | SARIMAX | ((0, 1, 0), (1, 0, 2, | ('amb_temp', 'wind_spd', 'bar_press') |
| | | ((0, 1, 1), (1, 0, 2, | ('amb_temp', 'wind_spd', 'sol_rad') |
| | | ((0, 1, 1), (2, 0, 0, | ('rel_hum', 'wind_spd', 'rainfall') |

4. CONCLUSION

This detailed analysis across multiple time series models and a variety of exogenous factors underlines the nuanced understanding required to effectively predict PM_{2.5} levels in urban settings like Delhi. The SARIMAX model, with its ability to incorporate external influences, stands out as particularly effective, offering significant potential for policymakers and environmental scientists in crafting more accurate air quality forecasts and better-informed pollution control strategies.

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