

## **Internal Model Controller for Conical Tank System**

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**Abstract:** *This manuscript proposes an internal model controller (IMC) for conical tank system with hybrid approach. The hybrid approach is the combination of lotus effect optimization (LEA) and attentive evolutionary generative adversarial network (AEGAN) algorithm; hence it is known as LEA-AEGAN approach. The main purpose of the work is to enhanced drainage of process fluid. Process fluids can be of various mixes of solids, semisolids, slurries, and liquids. The inclination angle of the tank aids drainage eliminates sediments, and so on, but it also adds non-linearity into the system. The IMC is used to non-linear systems, which is required to regulate the level of a conical tank. The proposed LEA is utilized to find the optimal controller parameters and minimize the error of the system. And the AEGAN is used to predicts the control parameters and ensure the controller tuning. By using the proposed system, it is implemented by MATLAB platform and compared with the existing techniques. The settling time, overshoot, and rise time of the proposed controller is 21.9sec, 11.11%, and 2.2sec, respectively.*

**Keywords:** *Internal Model Controller, Conical Tank System, Liquid Level, Gain Parameter, Set Point, Nonlinear System.*

### **1. INTRODUCTION**

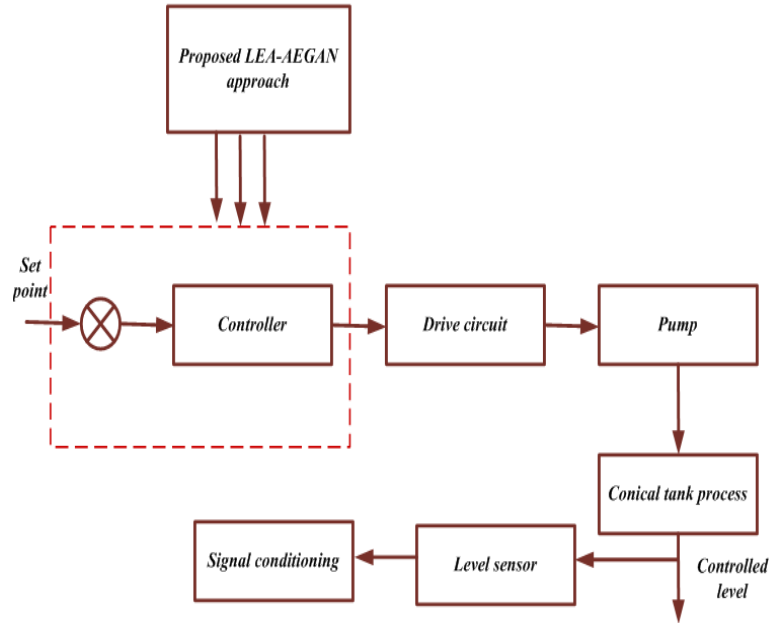
Conical tanks (CT) are non-linear due to their variable cross-sectional area [1]. For businesses utilizing non-direct cycles the regulator configuration is a difficult undertaking, since greater part of the control hypothesis manages straight interaction [2-3]. Numerous enterprises utilize proportional integral (PI) controller and relative basic subsidiary regulator as a result of its straightforward design and simple tuning [4]. They are ideal control for direct interaction. To achieve optimal process control, the proportional, integral, and derivative constants are set during controller tuning. The conical tank is profoundly non-linear. Be that as it may, solidness of the framework might be impacted [5]. To keep the level at the intended level, model-based controller design is used [6-7]. Ongoing advancements have been finished by the analysts to further develop the IMC-PID regulator exhibitions and vigor [8-9]. Time delay and constant time can be used to calculate the IMC-PID controller's tuning parameter. The maximum sensitivity ( $M_s$ ) assume significant part on account of model vulnerability or model confounds [10-11]. The model vulnerability happens principally because of cycle's boundaries varieties and nonlinearity of the cycles [12]. In this way, it is expected to plan powerful regulator which can perform well if there should be an occurrence of model vulnerability [13]. A few scientists have proposed  $M_s$ -based IMC-PID regulator for the different cycles with time delay [14]. A high level PID regulator which flowed with a lead-slack compensator, in view of IMC system for second-request processes in addition to dead time [15]. The acquired regulator shows generally excellent outcomes for the reference following alongside load change [16]. Direct combination is utilized to plan of lead-slack compensator connected in series with a PID regulator for all classes of cycles having no less than one shaft at the beginning in addition to time delay and the regulator's boundaries are chosen by changing tuning boundary  $\lambda$  for various vigor levels by assessing  $M_s$  esteem [17]. The goal of the proposed work is to use a process model to calculate the controller setting using model-based controller design [18], but the model's structure has not been explicitly used in the controller design. A process model is used in more detail in several alternative controller design approaches. Model reference versatile regulator emerges some solidness issue during ongoing

execution [19]. One of the strategies is IMC. The model of the cycle is run in lined up with the genuine interaction [20]. The open circle control plan method and the IMC plan strategy are exactly the same. Relatively speaking, the IMC structure's open circle control compensates for unnerving influences and model vulnerability.

Recent Research Work: A Brief Review Many studies have earlier occurred on the literatures which are depends on the control the conical tank level by IMC utilizing various techniques as well as aspects. Here, few of them are reviewed. R Rajesh [21] have used that the practicality of using a Fractional-order proportional-integral-derivative (FOPID) controller for gradually controlling the level of a single conical framework. It was one of the classic nonlinear control problems, and its design ensures that strong wastes don't leak out while also helping to mix fluids properly. This review, a double circle regulator was created and built with an expert interaction and slave process for a level control of a solitary tapered tank framework. The conical tank reference model and the traditional PID controller's output response were combined in the slave process and compared to the master process's output response. They got mistake signal was utilized to powerfully address the boundaries of the FOPID regulator in the expert cycle. The tuning of FOPID regulator was a provoking errand because of its presence of additional boundaries and it effectively did by PSO algorithm. M Kumar *et al.* [22] have introduced that An IMC-PI/PID regulator with a first or second request channel in series was intended for a few sorts of cycles with time delay. The tradeoff among execution and power was finished by changing the tuning boundary of the regulator. The current tuning strategy shows better exhibitions regarding overshoot (OS), settling time and ITAE mistake record. The effects of simulating various cycles were compared, and more recently, distributed tuning techniques have improved response times for set point changes and equivalent load changes. To remove the unfortunate overshoot, a set point weighting boundary 'b' was used, which was easier to select than a set point channel. The regulator's boundaries were fixed so that gives same strength level (Ms), by changing the tuning boundary. A 10% to 15% bother in every one of the boundaries of cycle models was acquainted with assess the vigor of the created tuning strategy. In the current review, a cone shaped tank framework was considered for the relevance of the introduced plan technique for PI/PID regulator. The PI controller was designed using the presented tuning strategy, which was then successfully applied to the conical tank's transfer function model and procedure. R Trivedi and P K Padhy [20] have fostered that backhanded fragmentary request approach, fragmentary request plant was moved in the recurrence area and the same plant was demonstrated by utilizing binomial guess. The same fragmentary request plant got was utilized for the plan of the regulator. While planning partial request regulators, heartiness and dealing with aversion to parametric varieties were of key significance. In this manner, circuitous fragmentary request approach was utilized which gives the adaptability to change the greatest responsiveness as per the framework prerequisites and wipes out the requirement for outside IMC channel. The used binomial expansion contributes to the achievement of the internal filter, and the proposed design method does not include an external IMC filter. A Ranjan and U Mehta [19] have fostered that the modified IMC that incorporates processes using a FOTDD. This technique was stretched out for each of the three sorts of interaction models, to be specific, incorporating in addition to , IFOPTD, IPTD and DIPTD. The criticism regulator was planned in an IMC system that can rapidly acquire from the plant boundaries. S K Vavilala *et al.* [21] have proposed that fractional-order IMC, for the level control of a cone shaped tank nonlinear framework. The engaged regulator has a partial channel flowed with a whole number request PID regulator. The FOIMC combines the advantages of fractional control, such as robustness, tuning parameter flexibility, and a large stability margin, with those of IMC, which include a stable controller and a small number of tuning parameters. Linearising the nonlinear framework incorporates the Lagrange leftover portion term to make up for the higher-request subordinates. The FOIMC controller's parameters were optimized with the help of the WOA and PSO algorithms. S Subramanian *et al.* [20] have proposed that different recognizable proof calculations were executed in the four-tank framework to exhibit the prevalence of the suggested subspace framework ID strategy for the different info plan. A framework recognizable proof strategy was used to distinguish the model of a unique framework.

Background of the recent research work: A general review of recent research indicates that for conical tank level systems, a model-based controller is essential. In comparison to the other controller, the suggested controller rejects disturbances more quickly, is more resilient to changes in gain, and uses less control energy. The system identification field is a challenging task in nonlinear systems. Numerous researchers are addressing this issue in the literature with regard to various technologies, including PSO, BNWOA, WOA, and N4SID. It has been shown that PSO has strong global search capabilities. The velocity equation, which uses the PSO algorithm, has stochastic variables, therefore the global best value varies arbitrarily. On the other hand, WOA is used to optimize the FOIMC controller parameters. To minimize the limitations of the dual tank system and achieve optimal control, the PID controller was tuned using BNWOA. N4SID is used to determine a dynamic system's model. The above

technologies are low set-point tracking, error is not reduced as better, and low performance is occurred. Liquid level regulation in conical tanks is therefore beyond the scope of the aforementioned technologies. Very few approaches-based works to address this issue have been published in the literature; these shortcomings and issues are what inspired this research effort. Configuration of Single Conical Tank System with Proposed Controller Fig.2 shows the configuration of single conical tank level system with proposed IMC. The framework that is being used is a conical tank, and because of the difference in the area of the cross segment of the level framework with level, it is very nonlinear. The rate of inflow into the tank is the governing factor. The process tank's level is the controlled variable. The sign molding unit, which creates the required sign for further handling, uses a level sensor to determine the level in the process tank. Through the use of a DAQ card, the cycle is connected to the PC. The computer functions as a regulator. The drive circuit receives the outcome from the PC. The drive circuit is made up of force electronic devices such as TRIAC, SCR, and others. The final control component can then be used to start the control move at that point. The controlling factor that keeps the desired level stable is the inflow rate into the tank.



**FIGURE 1.** Configuration of single conical tank level with proposed controller

Designing of Conical Tank System To facilitate communication and collect data, the level cycle station was used. As a regulator, the PC functions [28]. It includes the item that regulates the level interaction station. Process and reservoir tanks, the setup consists of a level sensor, I to P converter, a control valve, and pneumatic signals from the compressor. The level sensor first determines the real level values when the setup is activated. The signal is then transformed into a current signal between 4 and 20mA and sent to the computer via the data acquisition cord (DAC). The set point and the parameters entered in the regulator settings will determine the PC's next control move. The string is then used to return the sign that the PC sent to the station. The I to P converter is used to turn this signal into a pressure signal. Following a control value that modifies the water flow into the tank, the strain signal then controls the level. The tank is elevated above a stand and has a body made of hardened steel. To get to the storage tank, water enters the tank from above and passes through the base. Fig.2 shows the single system of conical tanks. A mathematical model is a system description that makes use of mathematical concepts and terminology. Making a mathematical model is the process of mathematical modeling. While non-linear systems require certain approximations to be solved, linear systems are typically modeled using direct derivations. Since Taylor's series technique is straightforward and precise within a specific range that is close to the steady state point, it is used here. Process companies face a fundamental problem with the control of fluid level and stream in the tank [18]. Pumping the liquids from one tank to another, where they are stored, is a requirement for the process industries. The fluid level in the tanks needs to be constantly observed even though it will be mixed or given chemical treatment on a regular basis. Controlling fluid level is a crucial and frequent task in process projects. The intended fluid level is kept constant in this level cycle, and the tank is shaped like a cone. The level control in the tapered tank is a difficult issue in light of its continually changing its cross-sectional region. The input flow into

the tank is managed to achieve this. The level of the tank and the inflow into the tank are the controlled variables. Many different process industries use conical tanks, including wastewater treatment, food processing, hydrometallurgical, and concrete mixing. A conical tank allows for better drainage of viscous fluids, semisolid materials, and solids.

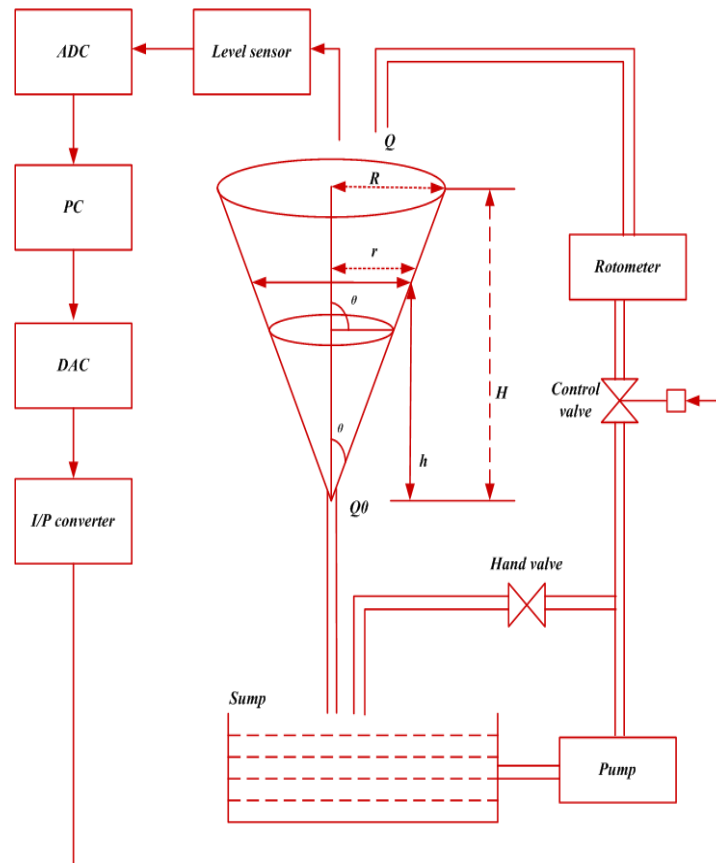


FIGURE 2. Single system of conical tanks

## 2. PROCESS DESCRIPTION

The PID controllers have been broadly utilized in the process businesses for a long time, because of their straightforwardness, adaptability and effectiveness. The tuning of a PID Regulator is essential, for the palatable activity of the cycle. Standard strategies for tuning incorporate Zeigler-Nichol's (ZN) extreme cycling technique, and Cohen-Coon's (CC) open circle tuning strategy. In both these techniques, the boundaries of the regulator are gotten for a working point, when the plant or cycle model is direct. This paper is primarily concerned with the design of IMC controllers for level control in the process of a conical tank. There is only one information and one result process in the conical tank framework. The cycle's outcome is the level, and the fluid's progression contributes to the interaction. One way to identify a non-straight framework is the conical tank framework. First rule differential condition is used to implement the tapered tank framework model. Simulink and the MATLAB ODE45 solver are used to resolve the differential condition. The outcomes are approved by utilizing the exchange capability model and Tribute reaction. Various tuning rules are utilized in the IMC controller's implementation to monitor the conical tank process's set point changes in level. The presentation list of various tuning rules is additionally acquired. The reenactment results demonstrated that IMC technique is a simple tuning and more viable method for upgrading soundness of time space execution of the conical tank framework shows the conical tank system's structure.

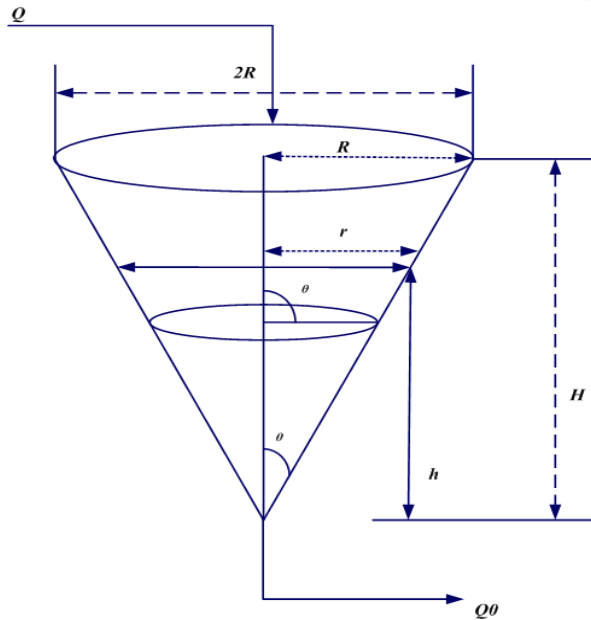


FIGURE 3. The conical tank system's structure

### 3. CONTROL STRUCTURE OF IMC

The generally distributed IMC tuning give unfortunate burden aggravation concealment to processes in which the ideal shut circle elements is fundamentally quicker than the open-circle elements [10]. The IMC channel is altered to determine low-request regulators that give powerful aggravation concealment regardless of the place where the unsettling influences enter the shut circle framework. For a really long-time engineers have attempted to foster better tuning rules for PID regulators. Notable IMC tuning decisions benefit from the fact that a single tuning boundary can achieve a fair balance between shut circle execution and the ability to highlight errors. The IMC tuning rules are educated to most undergrad substance designs and are broadly applied in industry. Notwithstanding, a few scholar and modern interaction control engineers have noticed that the broadly distributed IMC tuning rules, while giving satisfactory concealment of result unsettling influences, make a lackluster display smothering burden aggravations when the cycle elements are essentially more slow than the ideal shut circle elements. The solution suggested by Morari and colleagues was to play out the IMC plan technique while keeping in mind an additional integrator for the result aggravation. This strategy was found to give satisfactory burden aggravation concealment to many cycles and has been applied to display prescient control.

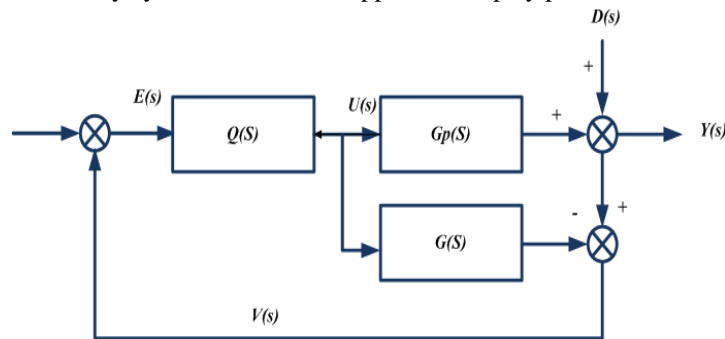


FIGURE 4. Control structure of IMC

In any case, the subsequent regulators don't have PID structure. Here we foster an IMC which give sufficient unsettling influence concealment independent of the place where the unsettling influence enters the shut circle framework. Consolidating ease lead in the IMC channel yields the tuning rules, which set limits for an IMC regulator in series with a channel. With today's control technology, these regulators are simple to install. The fundamental technique for cascade controller design was initially put forth and used by Brosilow and Markale. It yields results that are comparable to those of Morari and colleagues' method. Fig.4 shows the control structure of

IMC, Here,  $Q(s)$  is denoted as the IMC,  $G_p(s)$  is denoted as the process, The system's output, set-point, and external disturbance are represented by  $R(s)$ ,  $Y(s)$ , and  $D(s)$ , respectively.  $G(s)$  is designated as the process model.  $E(s)$  is denoted as Error,  $U(s)$  is denoted as Control input.

#### 4. LEA AEGAN ALGORITHM

Control the Level of Conical Tank and Reduce the Error Using LEA-AEGAN Algorithm

The LEA-AEGAN approach is proposed to reduce the error and control the level of liquid in conical tanks of the proposed system. The LEA is used for enhance the control factors of the controller, and reduce the error and AEGAN is used to predicts the control parameters. The following is a detailed description of the proposed approach.

Lotus Effect Optimization Algorithm (LEA)

The Lotus Effect Algorithm is a novel evolutionary algorithm that combines effective operators from the dragonfly algorithm, similar to how dragonflies move during flower pollination for exploration and how water's lotus effect—a self-cleaning characteristic on flower leaves—is used for extraction and local search operations [31]. The flowchart of lotus effect optimization algorithm is shown in Fig.5.

Step 1: Initialization

Step 2: Random Generation

Step 3: Calculation of Fitness Value

Step 4: Exploration Phase

Step 5: Exploitation Phase

Step 6: Update the Best Solution

Step 8: Termination

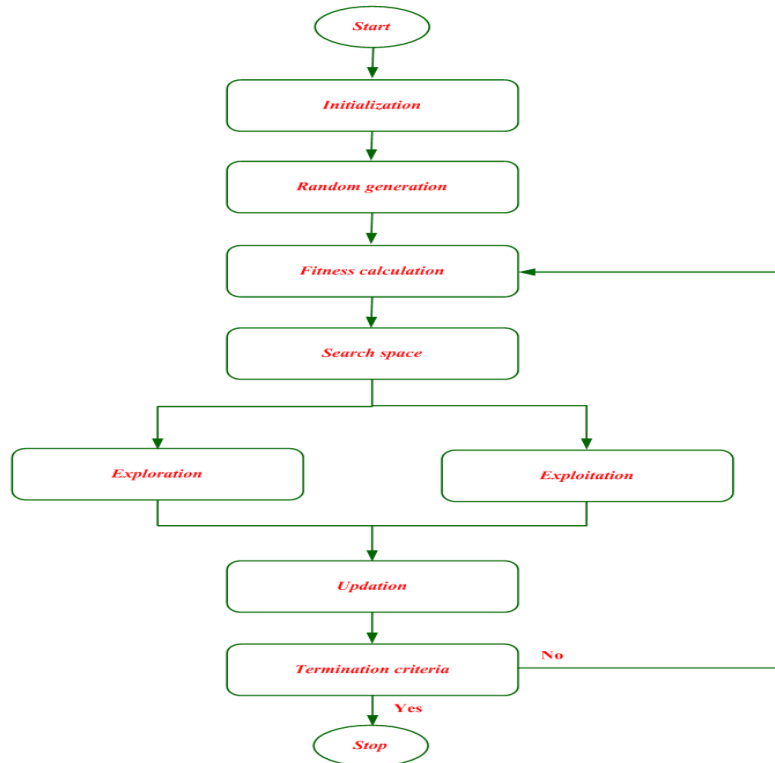


FIGURE 5. Flowchart of lotus effect optimization

## 5. RESULT AND DISCUSSION

The response for different controllers for the same step input for the conical tank process system transfer function

$$G(s) = \frac{Y(s)}{U(s)} = \frac{3.4641}{361.03631s + 1} \quad (1)$$

The conical tank process uses the implementation of IMC to monitor changes in load disturbance and step input changes in set point. In many chemical and biochemical industries, an integrating process is observed that has one or more poles at the transfer function model's origin. Because there is a pole at the origin the step response of these processes becomes unstable and it is difficult to control.

$$G_p = \frac{1e^{-4s}}{s(4s + 1)} \quad (2)$$

The analysis of first order delay integrating process. Subplot shows the set-point of the process. The process variable is occurring shows the load of the process. The load process is reached 5. It is weighted as minimize the set-point overshoot issue, and the process transfer.

Process industries like temperature control and level control use first order process delay time (FOPDT) processes extensively.

$$G(s) = \frac{1}{10s + 1} e^{-0.5s} \quad (3)$$

The analysis of 1<sup>st</sup> order plus time delay process. The set-point. The process set-point is reached as 1.2. Subplot shows the load of the regulatory response. The load is reached as 0.105. In the nominal case, the overshoot for the regulatory and servo problems is marginally higher than that of the other two methods; It is, however, less than that of the other two approaches when it comes to model uncertainty. As with the other methods, the maximum sensitivity (Ms) is set at 1.65 to allow for a fair comparison of robustness.

Consider the following UFOPDT which was also used by

$$G_p = \frac{1}{5s - 1} e^{-1s} \quad (4)$$

For a fair evaluation of the controller, the maximum sensitivity value Ms = 2.33 is selected in comparison to the other two approaches and the response for the unit set-point and load change. It can be reached as 1.9 and 0.59 respectively. In contrast to other approaches, the proposed method exhibits a quicker response time and reduced overshoot when dealing with servo problems.

Consider the following as SOPDT process

$$G_p = \frac{2e^{-1s}}{(10s + 1)(5s + 1)} \quad (5)$$

The analysis of stable second order delay process time. it shows the servo and regulatory problems in the controller as set-point and load as fast response. It allows to reach 1.1 and 0.149 respectively. In this method, the peak overshoot is reduced by a set-point weighting factor called "b" and a set point filter.

Consider SOPDT with inverse response.

Inverse response is seen in a number of chemical industry process units such as the exit temperature of a tubular exothermic reactor, the boiler drum level control by the heating medium flow rate, and the tray composition control of a distillation column by the vapor flow rate. For the process to display the inverse response, the transfer function's open right half plane needs to contain an odd number of zeros.

$$G_p = \frac{(-0.2s + 1)e^{-0.2s}}{(1s + 1)(1s + 1)} \quad (6)$$

The analysis of SOPDT with inverse response. It can also show the unit step change set-point as well as load change. It reached 1.19- and 0.45-unit response.

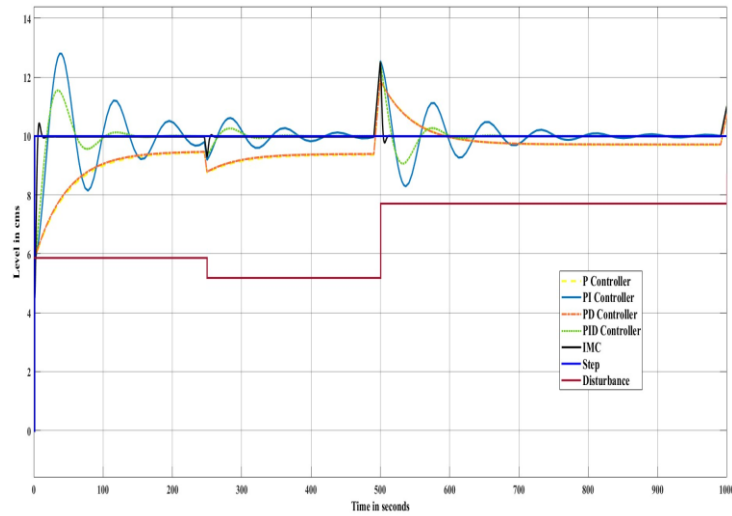


FIGURE 6. Controller's output response

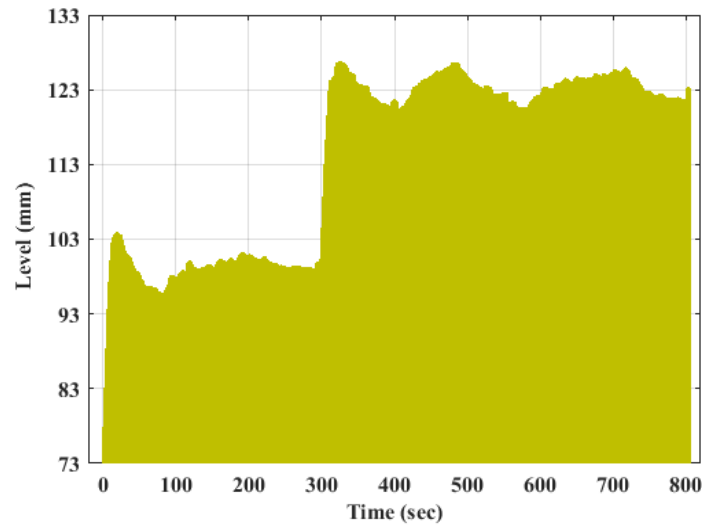


FIGURE 7. Analyses of IMC with conical tank

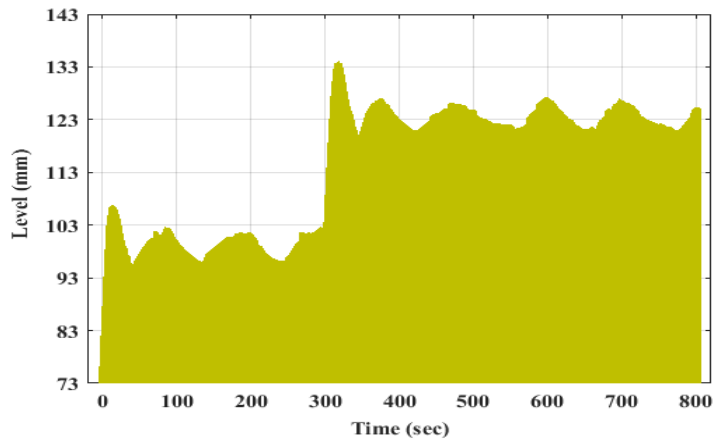


FIGURE 8. Analyses of existing PID controller with conical tank



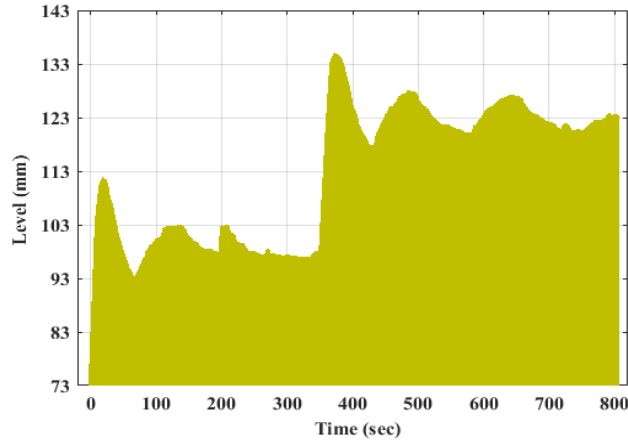


FIGURE 9. Analyses of existing PI controller with conical Tank

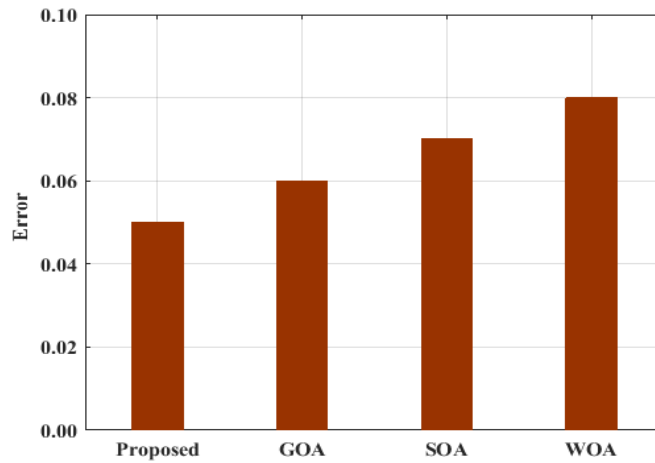


FIGURE 10. Comparison of error with proposed and existing systems Consider the unstable second order process.

$$G_p = \frac{2e^{-1s}}{(10s + 1)(5s + 1)} \tag{6}$$

The analysis of unstable second order delay process with set-point and load. It can reach to 1.2 and 0.4 respectively for control the unstable system. The answers indicate that there is more overshoot and settling time in the suggested approach. As a result, the current approach may be helpful in managing the unstable system and shows the analysis of flow rate for steady state and power. It shows the outlet flow rate as  $2.75 \times 10^4$  and power as  $2.6 \times 10^4$  the analyses of IMC with conical tank. The levels are raised to 123mm height. displays the analyses of existing PID controller with conical tank. It can be raised the level as 133.5mm height displays the analyses of existing PI controller with conical tank. It can be raised the level to 135mm height. Due to nonlinearity in the process, all three of the tuning methods used for level control exhibit oscillatory responses at first before becoming stable displays the error comparison of proposed and existing system. The proposed is 0.05, the GOA is 0.06, the SOA is 0.07, and the WOA is 0.08.

Evaluation criteria of different controller implemented for Conical Tank System Table 2 displays the various tuning rules are represented by the integral performance index for integral square error (ISE), integral absolutely error (IAE), and integral time absolute error (ITAE). We can examine the regulator method's lower ISE, IAE, and ITAE values in comparison to other tuning parameters by looking at Table 2.

**TABLE 1.** Tuning Methods for different controllers

Error Evaluation Criteria	ISE (sec)	IAE (sec)	ITAE (sec)
P controller	866.5	674	2.145e+05
PI controller	615	421.8	1.122e+05
PD controller	814	647.5	2.059e+05
PID controller	257	169	3.6245+04
IMC	520	135.5	3.65e+04

**TABLE 2.** Error Evaluation criteria for different controllers

Tuning Methods	P controller	PI controller	PD controller	PID controller	IMC
Settling time (sec)	470	500	245	190	21.9
Overshoot (%)	56	66	57	34.16	11.11
Rise time (sec)	154	14	140.17	14.1	2.2

The input tracking of conical tank system is achieved by using IMC with mild oscillations and within short period of time when compared with other that is the peak overshoot % of 11.123, is shown in Table 1. The IMC design process is the same as the open-loop control design process. Unlike open-loop control, the IMC structure takes disturbances and model uncertainty into account. The model uncertainty is adjusted for using the IMC tuning (filter) factor. It should be noted that while set point responses are the main focus of the standard IMC design procedure, set point responses are insufficient to guarantee effective disturbance rejection, particularly when disruptions originate at process inputs. A tweak was created to the IMC design process to enhance input disturbance rejection. *Robustness* is the capacity to tolerate uncertainty in a model and is high in IMC compared to others. From the both tables the performance of the proposed controller and proposed system is high performance, high stable and robustness.

## 6. CONCLUSION

A hybrid approach for tuning IMC with conical tank system is proposed. The main objective of the work is to achieve robust control of the conical tank system. The IMC is designed to ensure accurate tracking of set-points and robust disturbance rejection, even when unpredictability and disruptions are present. The proposed system is implemented by MATLAB platform and compared with the existing system. The error of the proposed, GOA, SOA, and WOA are 0.05, 0.06, 0.07, and 0.08, respectively. The settling time, overshoot, and rise time of the proposed controller is 21.9sec, 11.11%, and 2.2sec, respectively, which is low, when compared to the existing controllers. The various tuning rules ISE, IAE, and ITAE of the proposed controller is 520, 135.5, and 3.65e+04, respectively, which is low, when compared to the existing controllers. The proposed setup performs better than all other existing systems.

## REFERENCES

- [1]. Medewar, P. G., Sonawane, R. R., & Munje, R. K. (2017). Two tank non-interacting liquid level control comparison using fuzzy and PSO controller. In *National Conference on Emerging Trends in Engineering & Technology* (Vol. 1, pp. 24-31).
- [2]. Davis, I., Jishnu, C. P., William, R., Krishnan, S., Sumith, K., & Sathyan, M. K. (2017). N, Level Control of two conical tank non interacting system using PID and Fuzzy Logic. *International Journal of Innovative Research in Electrical, Electronics, Instrumentation and Control Engineering*, 5(4), 35-42.
- [3]. Mukherjee, A., Chakraborty, N., & Das, B. K. (2017, April). Whale optimization algorithm: An implementation to design low-pass FIR filter. In *2017 Innovations in Power and Advanced Computing Technologies (i-PACT)* (pp. 1-5). IEEE.
- [4]. Prasad, D., Mukherjee, A., Shankar, G., & Mukherjee, V. (2017). Application of chaotic whale optimisation algorithm for transient stability constrained optimal power flow. *IET Science, Measurement & Technology*, 11(8), 1002-1013.

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- [5]. Febina, C., & Vijula, D. A. (2020). Model based controller design using real time neural network model and PSO for conical tank system. *Journal of Control Engineering and Applied Informatics*, 22(3), 13-24.
- [6]. Zhang, B., Sun, X., Liu, S., & Deng, X. (2019). Recurrent neural network-based model predictive control for multiple unmanned quadrotor formation flight. *International journal of aerospace engineering*, 2019, 1-18.
- [7]. Eswaran, T., & Kumar, V. S. (2017). Particle swarm optimization (PSO)-based tuning technique for PI controller for management of a distributed static synchronous compensator (DSTATCOM) for improved dynamic response and power quality. *Journal of applied research and technology*, 15(2), 173-189.
- [8]. Christudas, F., & Dhanraj, A. V. (2020). System identification using long short term memory recurrent neural networks for real time conical tank system. *Rom. J. Inf. Sci. Technol.*, 23, 57-77.
- [9]. Saxena, S., & Hote, Y. V. (2019). Design and validation of fractional-order control scheme for DC servomotor via internal model control approach. *IETE Technical Review*, 36(1), 49-60.
- [10]. Sánchez, H. S., Padula, F., Visioli, A., & Vilanova, R. (2017). Tuning rules for robust FOPID controllers based on multi-objective optimization with FOPDT models. *ISA transactions*, 66, 344-361.
- [11]. Vijayalakshmi, S., Manamalli, D., & PalaniKumar, G. (2014). Closed loop experimental validation of linear parameter varying model with adaptive PI controller for conical tank system. *Journal of Control Engineering and Applied Informatics*, 16(4), 12-19.
- [12]. Horla, D., & Sadalla, T. (2020). Optimal tuning of fractional-order controllers based on Fibonacci-search method. *ISA transactions*, 104, 287-298.
- [13]. Begum, K. G., Rao, A. S., & Radhakrishnan, T. K. (2017). Enhanced IMC based PID controller design for non-minimum phase (NMP) integrating processes with time delays. *ISA transactions*, 68, 223-234.
- [14]. Arya, P. P., & Chakrabarty, S. (2018). IMC based fractional order controller design for specific non-minimum phase systems. *IFAC-PapersOnLine*, 51(4), 847-852.
- [15]. Pachauri, N., Yadav, J., Rani, A., & Singh, V. (2019). Modified fractional order IMC design based drug scheduling for cancer treatment. *Computers in biology and medicine*, 109, 121-137.
- [16]. Verma, B., & Padhy, P. K. (2019). Indirect IMC-PID controller design. *IET Control Theory & Applications*, 13(2), 297-305.
- [17]. Travieso Torres, J. C., Duarte Mermoud, M., & Beytia, O. (2017). Combining fractional order operators and adaptive passivity-based controllers: an application to the level regulation of a conical tank.
- [18]. Abinaya, N., DivyaPriya, A. V., Yazhini, J., & Nandhini, K. M. (2018). Fractional Order IMC-PID Controller Design for Non-Linear System. *proc. of IJIREICE*, 6(1).
- [19]. Birs, I., Muresan, C., Nascu, I., & Ionescu, C. (2019). A survey of recent advances in fractional order control for time delay systems. *Ieee Access*, 7, 30951-30965.
- [20]. JAYAKAR, S. A., & VINODHINI, G. Real Time Implementation Of IMC Based PID Controller for Conical Tank Level Control Process.
- [21]. Rajesh, R. (2019). Optimal tuning of FOPID controller based on PSO algorithm with reference model for a single conical tank system. *SN Applied Sciences*, 1(7), 758.
- [22]. Kumar, M., Prasad, D., & Singh, R. S. (2023). Level Control in Conical Tank Using IMC-PID Controller. *Journal of Engineering Science & Technology Review*, 16(2).
- [23]. Amuthambigaiyin Sundari, K., & Maruthupandi, P. (2022). Optimal design of PID controller for the analysis of Two TANK system using metaheuristic optimization algorithm. *Journal of Electrical Engineering & Technology*, 17(1), 627-640.
- [24]. Trivedi, R., & Padhy, P. K. (2020). Design of indirect fractional order IMC controller for fractional order processes. *IEEE Transactions on Circuits and Systems II: Express Briefs*, 68(3), 968-972.
- [25]. Ranjan, A., & Mehta, U. (2022). Fractional filter IMC-TDD controller design for integrating processes. *Results in Control and Optimization*, 8, 100155.
- [26]. Vavilala, S. K., Thirumavalavan, V., & Chandrasekaran, K. (2020). Level control of a conical tank using the fractional order controller. *Computers & Electrical Engineering*, 87, 106690.
- [27]. Subramanian, S., Chidhambaram, G. B., & Dhandapani, S. (2021). Modeling and Validation of a Four-Tank System for Level Control Process Using Black Box and White Box Model Approaches. *IEEJ Transactions on Electrical and Electronic Engineering*, 16(2), 282-294.
- [28]. Li, D., Liu, L., Jin, Q., & Hirasawa, K. (2015). Maximum sensitivity based fractional IMC-PID controller design for non-integer order system with time delay. *Journal of Process Control*, 31, 17-29.
- [29]. Wang, Q., Lu, C., & Pan, W. (2016). IMC PID controller tuning for stable and unstable processes with time delay. *Chemical engineering research and design*, 105, 120-129.
- [30]. Begum, K. G., Rao, A. S., & Radhakrishnan, T. K. (2016). Maximum sensitivity based analytical tuning rules for PID controllers for unstable dead time processes. *Chemical engineering research and design*, 109, 593-606.
- [31]. Dalirinia, E., Jalali, M., Yaghoobi, M., & Tabatabaee, H. (2023). Lotus effect optimization algorithm (LEA): a lotus nature-inspired algorithm for engineering design optimization. *The Journal of Supercomputing*, 1-39.
- [32]. Wu, Z., He, C., Yang, L., & Kuang, F. (2021). Attentive evolutionary generative adversarial network. *Applied intelligence*, 51, 1747-1761.
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