

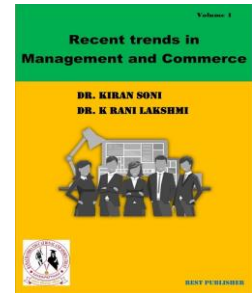


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Mutual Funds Evaluation and Selection Using GRA Method

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Abstract

The mutual fund industry has expanded exponentially, particularly in the last two decades of the 20th century. Accurate economic performance ratings allow for contrasts between managers of investments and make it simpler for average investors to select top managers. Due to greater market competition, fund managers must work harder to win over investors and management. As a result, it is crucial that investors and fund managers both frequently assess the efficacy of mutual fund investments. The most recent data indicates that this industry is currently managing 6.8 trillion rupees worth of assets. On the Indian market, there are presently more than a thousand mutual fund plans, with some of them providing higher returns than others. To assess the efficiency of equity-based mutual funds This essay was written with effort. forty-five initiatives from two both private and two public sector groups were examined between April 1997 and April 2012. (15 years). The pricing model for capital assets and a risk-return connection were both used in the analysis. (CAPM). The best two performers, according to the overall analysis, are HDFC and ICICI, with the bottom two performers being UTI and LIC. As a consequence, the risk-return relationship's predicted return was lower. The outcomes also demonstrate that some initiatives, which dealt with the issue of diversification, do not perform well. Sensex Plan is the best scheme in the data set according to the MCDM GRA technique, while Top 100 Fund is the worst scheme.

Keywords: Mutual Funds, GRA technique

Introduction

With the popularity of mutual funds increasing, performance evaluation of investment initiatives has become an absolutely crucial subject. A powerful tool for researchers to evaluate the efficient the marketplace hypothesis is the systematic assessment of fund performance, which allows peer comparison between investment managers, aids typical investors in spotting skilled managers, helps supervisors monitor behavior efficiently, and facilitates peer contrast among expenditure managers. The mutual fund industry has expanded exponentially, particularly in the last two decades of the 20th century. Due to the entry of private mutual funds, the company experienced a shift from a public sector monopoly to an independent monopolistic industry. (since 1993). A methodical evaluation strategy reduces confusion and helps small investors decide how much to invest in various mutual fund schemes. Due to greater market competition, fund managers must work harder to win over investors and management. As a result, it is crucial that investors and fund managers both frequently assess the performance of mutual funds. Several investors can invest in securities like stocks, bonds, short-term money market instruments, and other types of investments through a mutual fund, which is a professionally managed collective investment plan. Investors favor mutual funds for a variety of factors. Directly buying stocks off the market is one way to trade. however, confirm the operation of the prospectively acquired company. Understanding the company's potential for future business success, the promoter's track record, and the dividend requires study into past for bonus payments. Before making an investment, one should finish their research. Nevertheless, lots of stock market buyers Prior to investing, it requires time and effort to collect a lot of information. As a consequence, investors prefer the mutual fund route. Following thorough research and analysis, they accept the responsibility of investing in stocks through a mutual fund plan. An investor does not need to trouble researching hundreds of stocks. The qualified fund management team of the mutual fund is in control. Indian mutual fund history began in 1963, when UTI was established by a parliamentary order. As of April 30, 2012, there were 1292 mutual fund schemes in India, with a total market valuation of Rs. 6,80,154 crores. (also known as assets under management). The typical individual still doesn't understand how mutual fund schemes operate today. And it makes sense to research conduct. Looking at the risk-return relationship is one of the best ways to judge a mutual fund's performance.

The timing of anticipated returns cannot be altered by unconditional techniques. These fund activities are routine. As a result, it disregards the timetables of fund managers because it assumes risk remains constant over time. Due to time

variation, beta (systematic risk) is not time invariant in regularly managed funds. time-related factors, changes in market prices, and major variations in fund inflows and outflows beyond the fund manager's control This may shift if the portfolio changes. new information about the economy in general and/or a particular company, as well as the relative risk of the firm; this, in turn, can change their expected income. Financial instrument volatility and investor hopes The finance literature acknowledges that time differs. (Coggins et al., 2004). Under the conditional performance evaluation method, the risk exposures of the Fund Manager and related market premiums change over time in accordance with the state of the economy. Consequently, when assessing the success of funds, the time variation of investment risk should be considered. (Merton, 1971). Other fresh models for conditional performance assessment were motivated by this concept. This suggests that the funds' estimated return and risk will change over time. The state of the economy has been established and is measured using variables linked to public knowledge. An indicator of success is conditional alpha. The excess returns of a fund and based on variables with available information The strategy differs from other methods because it aims to replicate the long-term risk characteristics of the fund. Assessment of Conditional Performance, This generally complies with market efficiency's semi-strong form³. (Fama, 1970). If the market is efficient, a fund manager cannot raise the worth of stocks using a machine trading strategy. a manager should offer higher returns compared to a machine trading strategy if he or she is to contribute value and produce positive conditional alpha. Ferson and Schott (1996) estimated anticipated performance using historical average returns. They employ performance metrics that are dependent on public information variables to prevent induced bias. by using profitable investment managers who depend on the information available The performance wasn't the best, in my view. As a result, conventional performance measures that assume constant risk can only attribute extraordinary performance to a strategy when based on general information. Public information has a temporal lag caused by macroeconomic variables and is a linear function of mutual fund beta. They only offer a small number of performance measures.

A businessman invests his money, and the bank's financial success can be evaluated using the MCDM method. Additionally, it qualifies as the top performing bank. MCDM is a well-defined instrument that compares a company's performance to that of sector leaders and is used for improving weaknesses. Determine the strategies employed by industry stars to achieve their performance levels in order to raise one's own performance. wisely applies this information. Net Profit Ratio Like the long-term funding rate, ratio The multiple criteria decision making (MCDM) approach Using different financial indicators, List a number of Indian private sector institutions. To take into account mutual fund results An attempt was undertaken in this study. Giving priority to private sector banks serves two purposes: first, it sets a standard for other banks to strive for, and second, it allows investors to pool their money in mutual funds with the best banks.

Mutual Funds

The public can buy shares from a joint fund. Like any other business, a trust raises money from clients by selling shares of the fund. Various bonds were issued using funds collected through stocks, bonds, money markets, and commodities. Financial objectives are comparable for each mutual fund. And the money is invested to achieve the fund's objective and carry out its investment plan. A professional financial manager is in charge of managing this fund's trading operations as well. Every mutual fund investor shares in the fund's profit or loss equally. (based on the total number of owned shares). Depending on their interests and risk tolerance, any investor can diversify their portfolio by investing a small amount in a number of different sectors. In 2003, Roy et al. conducted an empirical research on the conditional performance of Indian mutual fund investments using the unrestricted and conditional models from ICICI, HDFC, LIC, and UFI. In this study, the success of many mutual funds is assessed. When evaluating the effectiveness of mutual fund administrators The effect of including lagging informative data is investigated in the Indian setting. using variables with lag information as a prerequisite improves the success of mutual fund schemes. Success in the mutual fund industry depends on gaining the trust of clients. To improve investors' confidence in investing in mutual funds, A minimum guaranteed income, financial incentives, and transparency in the services provided to them Ensure reliability of efficiency, etc. Depending on education, employment status, and family's yearly revenue The research identifies the crucial elements. to spend money on mutual funds A minimal guaranteed return, followed by transparency and stability, is what will regain the investor's trust. It draws buyers to mutual fund investments. Numerous characteristics exist in different mutual fund schemes. These characteristics include their past success, a history of dividend payments, the possibility of income stability, etc. According to investor rankings, past performance is the main attraction for buyers when selecting a mutual fund plan.

The entrance barrier for investing in mutual fund schemes has recently been removed, according to mutual fund companies. Generally speaking, responses are mutual funds. And the study found that engaging in a systematic investment plan is somewhat influenced. The removal of entry burden only has a significant impact on a small number of people. Most investors assess mutual funds' success before making an investment. There are numerous ways to assess the effectiveness of various mutual fund plans. The absolute return of funds is greater than the returns of other similar schemes, according to the survey's majority of respondents, who used it as a benchmark for assessing the performance of mutual fund schemes. And wish to make a withdrawal. Evaluation of any fund's performance is less favored. The research also demonstrates the correlation between fund returns and benchmark market index returns. a collection of information used to evaluate the efficiency of Indian mutual funds Examples are provided in this part. The techniques

used to arrive at the final performance evaluation findings are also thoroughly discussed. The variables used and their importance to the mutual fund industry are also explained for the readers' improved understanding. The beta value of any investment is calculated in the pricing model for capital assets in order to assess its risk. It assesses an asset's risk in connection to the market. If the beta value of a project is higher than one, it is considered riskier than the market index. Only one scheme, UTI's banking industry fund, has a higher beta in this review of 12 projects. Despite the elevated risk, it was 9% higher. The asset's beta risk measure and After determining the annual growth rate of the market index, we calculate the anticipated rate of return for a mutual fund plan. 1997 to 2012, the study's timeframe. There are a total of 45 share-based mutual fund plans that are considered. PSUs own ten of the twelve, including LIC and UTI. The remaining portion is held by ICICI and HDFC and is in the private sector. The benchmark stock indices NIFTY and SENSEX, as well as the daily closing net asset values (NAV) of mutual funds, were used in the research to calculate risk. The main concept of the study is to predict a project's expected return (risk adjusted) and then contrast that prediction with the project's real rate of return over time.

GRA method

In many areas, Multi-Criteria Decision Making (MCDM) is quick. An expanding issue Among the places. How to assess a collection of alternatives based on various criteria is the main issue. Despite the fact that this issue is very real, there are some solutions, and it can be challenging to assess their quality. Multiple Targets are taken into consideration simultaneously for optimization in multi-criteria decision-making models. Each objective's measure is for other goals. Size can change. For instance, increasing profitability, which is gauged in terms of money, could be a goal. Reducing labor time could also be a goal. However, not all of these goals are in the same path, and sometimes they conflict with one another. Superior decision-making in this area comes from superior programming. Due to its significance and practical use, a description of multi-criteria decision-making models is provided below. The most suitable of based on n factors for decision available options alternative methods of selection or ranking, and decision-making processes that consider multiple factors and are common to the group. There are different multi-criteria techniques to help with selection in situations where there are multiple criteria. The gray theory was first proposed by Professor Zhulong Deng in 1982 to address circumstances marked by partly known and partially unknown knowledge. According to the Gray theory, a system is referred to as a "white system" when all of its information is known, and as a "black system" when all of its information is unclear. In a gray structure, knowledge is only partially known. Gray theory is a method for investigating uncertain information and is very good for mathematical study of systems with uncertain information. With partial and discrete data, it is a helpful method for resolving ambiguous problems. The five main elements of the theory are gray prediction, GRA, gray decision, gray programming, and gray administration.

GRA, which is developed from Gray system theory, is a quantitative method for determining the relationship between sequences using a limited amount of data. The core idea behind GRA is that the degree of similarity between two sequence curves' geometric patterns establishes how close a relationship is. The more similar the curves are to one another, the stronger the connection between the series is, and vice versa. GRA is effective at resolving problems involving complex interrelationships between many different elements and factors. It has been successfully applied to solve various MCDM challenges such as employee selection facility layout and dispatch, hiring decisions, identification of silicon wafer cutting defects, restoration planning for power distribution systems, the study of the integrated-circuit marking process, quality function installation modeling, supplier selection, etc. The first step in the GRA procedure is to normalize each alternative's performance. In this stage, the original array is changed into a duplicate array. The correlation between the ideal and real normalized sequences is then ascertained using an allusion pattern (the ideal target sequence) as an indicator. The gray association score between every compared genome and the reference sequence is then determined using these gray indices of correlation. The gray correlation coefficient reveals the degree of interconnection between the reference and comparative sequences. A greater correlation between the comparison and standard sequences is indicated by a larger gray correlation coefficient. If the two rows match, the matching gray scale's number is equal to one. In all other situations, it is better to use alternatives with a high gray relative grade.

TABLE 1. Given evaluation parameter

C1	risk factor(beta)
C2	annual return on market
C3	expected rate of return
C4	actual rate of return

TABLE 2. Data Set for Economic feasibility TOPSIS method

HDFC 1	growth fund
HDFC 2	children fund
HDFC 3	sensex plan
ICICI 1	dynamic plan
ICICI 2	banking and financial
ICICI 3	services industries fund
UTI 1	UTI top 100
UTI 2	banking sector fund
UTI 3	equity fund
LIC 1	top 100 fund
LIC 2	tax plan
LIC 3	sensex advantage growth

Table 2 shows the alternatives (schemes) growth fund is HDFC 1 , children fund is HDFC 2, senssex plan is HDFC 3, dynamic plan is ICICI 1, banking and financial is ICICI 2, services industries fund is ICICI 3, UTI top 100 is UTI 1, banking sector fund is UTI 2, equity fund is UTI 3, top 100 fund is LIC 1, tax plan is LIC 2, senssex advantage growth is LIC 3.

Table 3. Data Set for mutual fund TOPSIS method

	C1	C2	C3	C4
HDFC 1	0.79	18.77	10.51	26.52
HDFC 2	0.36	18.35	11.73	14.88
HDFC 3	0.95	18.32	17.80	30.47
ICICI 1	0.75	20.14	17.11	27.52
ICICI 2	0.93	5.74	5.90	16.69
ICICI 3	0.82	10.70	10.19	8.14
UTI 1	0.83	5.24	5.71	6.43
UTI 2	1.02	4.98	4.92	14.00
UTI 3	0.69	4.85	5.83	11.45
LIC 1	0.93	12.59	12.27	6.67
LIC 2	0.85	12.85	12.12	8.09
LIC 3	0.85	5.43	5.82	0.01

Table 3 show the Data set of the growth fund, children fund, senssex plan, dynamic plan, banking and financial, services industries fund, UTI top 100, banking sector fund, equity fund, top 100 fund, tax plan, senssex advantage growth of the C1, C2, C3, C4, and C5.

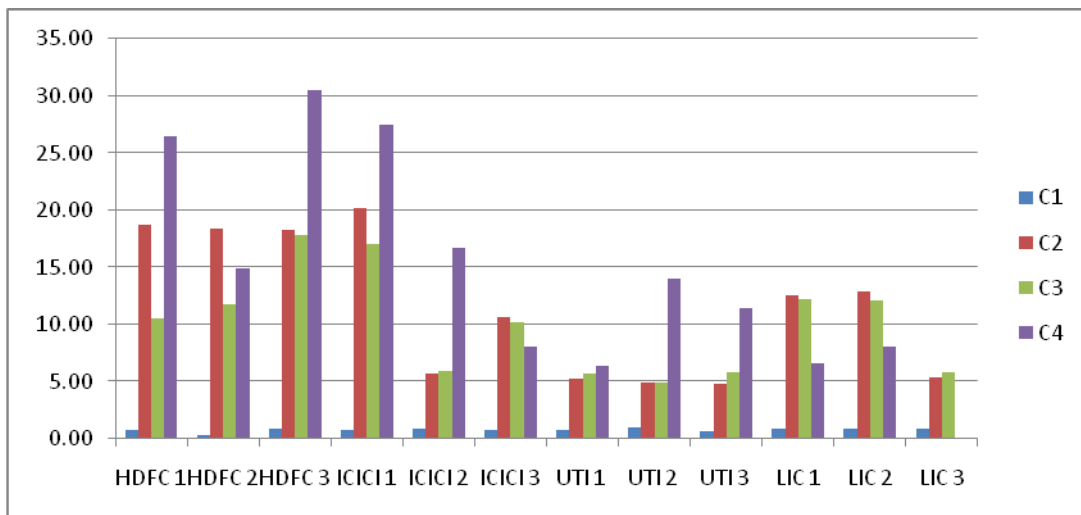


FIGURE 1. data set graph

Figure 1 shows that the Data set of the growth fund, children fund, sensex plan, dynamic plan, banking and financial, services industries fund, UTI top 100, banking sector fund, equity fund, top 100 fund, tax plan, sensex advantage growth of the C1, C2, C3, C4. HDFC Is Give High Values and UTI & LIC is low values.

TABLE 4. Normalized Data

	C1	C2	C3	C4
HDFC 1	0.3485	0.0896	0.5662	0.1297
HDFC 2	1.0000	0.1171	0.4717	0.5118
HDFC 3	0.1061	0.1190	0.0000	0.0000
ICICI 1	0.4091	0.0000	0.0543	0.0968
ICICI 2	0.1364	0.9418	0.9240	0.4524
ICICI 3	0.3030	0.6174	0.5910	0.7331
UTI 1	0.2879	0.9745	0.9387	0.7892
UTI 2	0.0000	0.9915	1.0000	0.5407
UTI 3	0.5000	1.0000	0.9296	0.6244
LIC 1	0.1364	0.4938	0.4296	0.7814
LIC 2	0.2576	0.4768	0.4410	0.7347
LIC 3	0.2576	0.9621	0.9305	1.0000

Table 4 shows the data from which the normalized data is calculated from the data set value is divided by the sum of the square root of the column value. It is the Normalization of Data set of the growth fund, children fund, sensex plan, dynamic plan, banking and financial, services industries fund, UTI top 100, banking sector fund, equity fund, top 100 fund, tax plan, sensex advantage growth of the C1,C2,C3,C4.

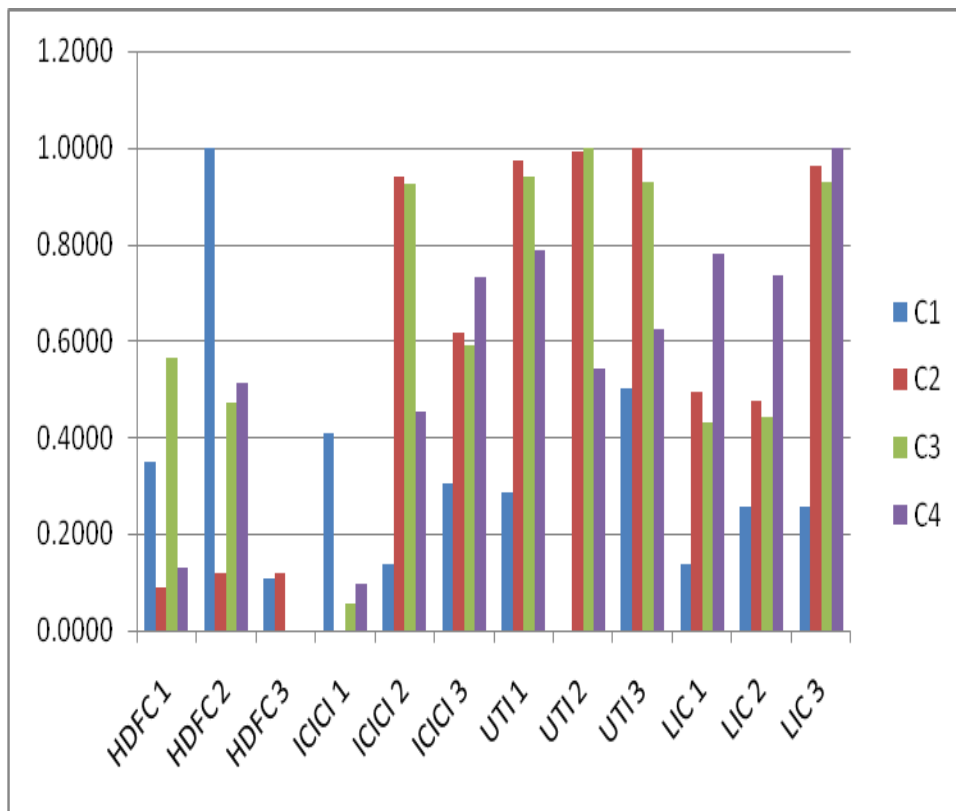


FIGURE 2. Normalized Data

Figure 2 shows the data from which the normalized data is calculated from the data set value is divided by the sum of the square root of the column value. It is the Normalization of Data set of the growth fund, children fund, sensex plan, dynamic plan, banking and financial, services industries fund, UTI top 100, banking sector fund, equity fund, top 100 fund, tax plan, sensex advantage growth of C1,C2,C3,C4.

TABLE 5. Deviation sequence

	C1	C2	C3	C4
HDFC 1	0.6515	0.9104	0.4338	0.8703
HDFC 2	0.0000	0.8829	0.5283	0.4882
HDFC 3	0.8939	0.8810	1.0000	1.0000
ICICI 1	0.5909	1.0000	0.9457	0.9032
ICICI 2	0.8636	0.0582	0.0760	0.5476
ICICI 3	0.6970	0.3826	0.4090	0.2669
UTI 1	0.7121	0.0255	0.0613	0.2108
UTI 2	1.0000	0.0085	0.0000	0.4593
UTI 3	0.5000	0.0000	0.0704	0.3756
LIC 1	0.8636	0.5062	0.5704	0.2186
LIC 2	0.7424	0.5232	0.5590	0.2653
LIC 3	0.7424	0.0379	0.0695	0.0000

Table 5 shown that the deviation sequence values and is calculated that the formulas.

TABLE 6. Grey relation coefficient

	C1	C2	C3	C4
HDFC 1	0.4342	0.3545	0.5355	0.3649
HDFC 2	1.0000	0.3616	0.4863	0.5060
HDFC 3	0.3587	0.3621	0.3333	0.3333
ICICI 1	0.4583	0.3333	0.3458	0.3563
ICICI 2	0.3667	0.8957	0.8681	0.4773
ICICI 3	0.4177	0.5665	0.5501	0.6520
UTI 1	0.4125	0.9515	0.8908	0.7035
UTI 2	0.3333	0.9833	1.0000	0.5212
UTI 3	0.5000	1.0000	0.8766	0.5711
LIC 1	0.3667	0.4969	0.4671	0.6958
LIC 2	0.4024	0.4887	0.4721	0.6534
LIC 3	0.4024	0.9295	0.8779	1.0000

A zeta value is constant and a value of 0.5. Table 6 is given for a grey relation coefficient shown in figure 3.

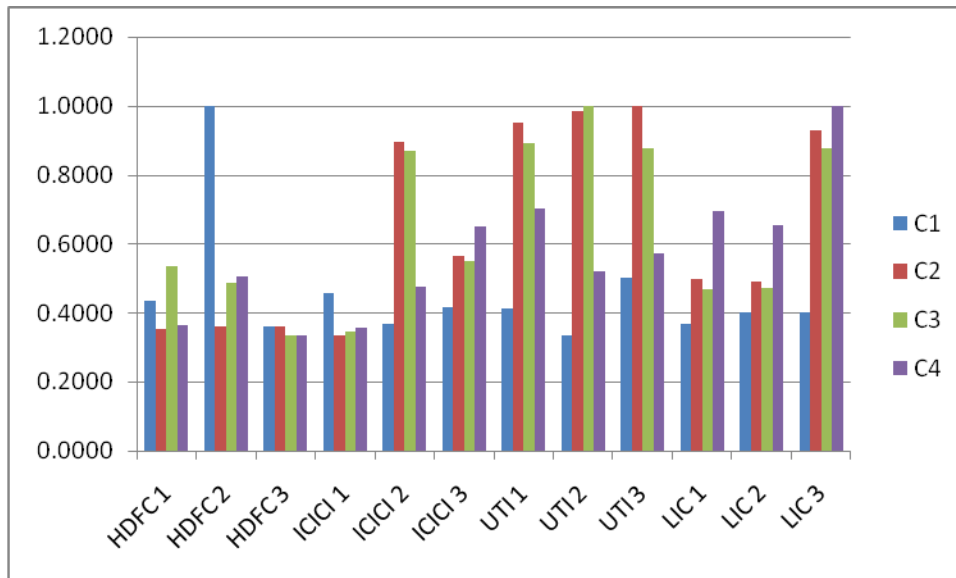


FIGURE 3. Grey relation coefficients

TABLE 7. GRA values and rank

HDFC 1	0.4223	10
HDFC 2	0.5884	6
HDFC 3	0.3469	12
ICICI 1	0.3735	11
ICICI 2	0.6519	5
ICICI 3	0.5466	7
UTI 1	0.7396	2
UTI 2	0.7095	4
UTI 3	0.7369	3
LIC 1	0.5066	8
LIC 2	0.5041	9
LIC 3	0.8025	1

Obtained by using formulas to calculate the GRA values, the result of the method was shown above. LIC 3 is highest values for GRA result and HDFC 3 lowest values for GRA result showing in figure 4. Table 7 shows the LIC 3 is on 1st rank, UTI 1 is on 2nd rank, UTI 3 is on 3rd rank, UTI 2 is on 4th rank, ICICI 2 is on 5th rank, HDFC 2 is on 6th rank, ICICI 3 is on 7th rank, LIC 1 is on 8rd rank, LIC 2 is on 9th rank, HDFC 1 is on 10th rank, ICICI 1 is on 11th HDFC 3 is on 12th rank.

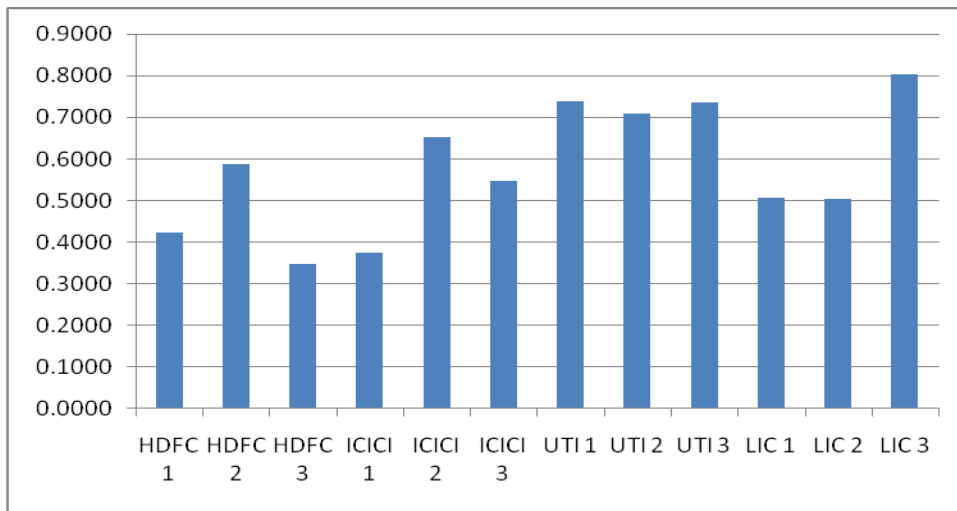


FIGURE 4. shown that the graph about GRA values

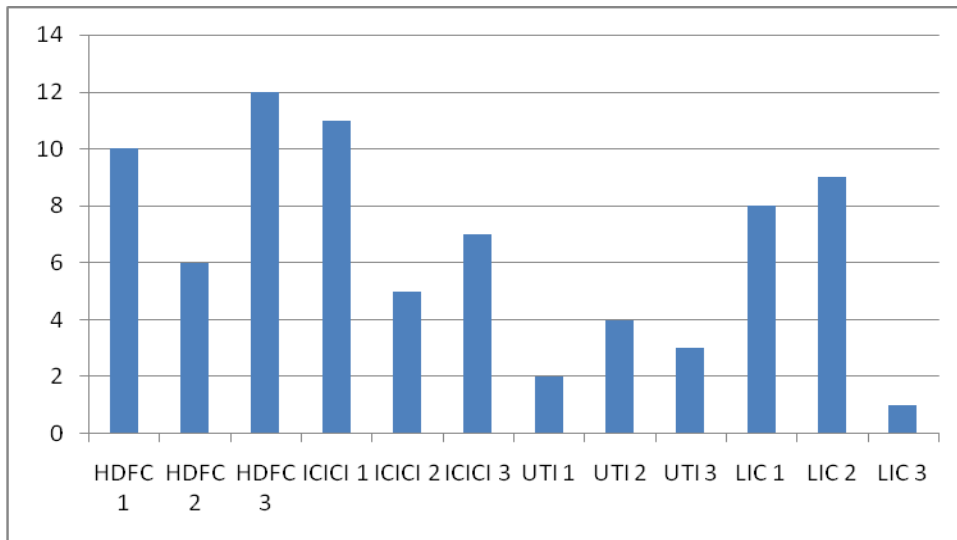


FIGURE 5. Rank mutual funds GRA method

Figure 5 shows the LIC 3 is on 1st rank, UTI 1 is on 2nd rank, UTI 3 is on 3rd rank, UTI 2 is on 4th rank, ICICI 2 is on 5th rank, HDFC 2 is on 6th rank, ICICI 3 is on 7th rank, LIC 1 is on 8rd rank, LIC 2 is on 9th rank, HDFC 1 is on 10th rank, ICICI 1 is on 11th HDFC 3 is on 12th rank. First rank is very worst benefit schemes for the data set so LIC 3 is worst scheme in the data set. Last rank is best mutual fund scheme in the data set so HDFC 3 is best scheme.

Conclusion

The performance of mutual funds was evaluated in the study between 1997 and 2012 using data from 12 mutual fund schemes. This study uses conditional models to estimate performance. Indian mutual fund managers are strong the study reveals that they have good stock picking skills. The study uses MCDM to look into the performance of equity-based mutual fund schemes in India. Private sector businesses have consistently outperformed those in the public sector. While HDFC and ICICI have performed well, UTI is bad. Among LIC's 2 mutual fund schemes, neither plan worked well. On the other hand, in 3 schemes of ICICI and HDFC are highly efficient. 3 out of 2 schemes of LIC are average performers, because most of its projects have delivered expected returns. In the last 15 years, Private Sector Mutual Funds (HDFC and ICICI) the results clearly show that PSUs (LIC and UTI) have outperformed. Although HDFC and ICICI mutual funds are less risky, Analysis shows that LIC is very risky. This is one of the causes of LIC's subpar performance. Private sector mutual fund schemes are less hazardous than public sector ventures, and the analysis generally indicated that they are more successful. The first rank for the dataset is the worst utility project, so the LIC sensex advantage growth in the data set are the worst projects. The last ranked mutual fund scheme in the data set is, so sensex plan is best plan.

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